

Today Jan 15 Sections 12.5-12.7

Tuesday 1/16 tutoring with Ali in eppy 107 7:00-8:30

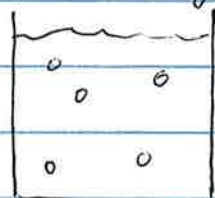
Wednesday 1/17 Section 12.4 and 12.8 and catch up

Friday 1/19 start chapter 13

### Colligative properties

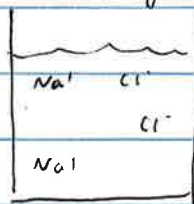
properties of solutions that depend on the amount of particles in solution

non-electrolyte



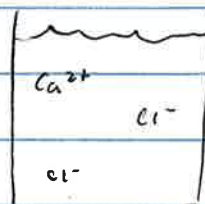
0  $C_{12}H_{22}O_{11}$

electrolyte



1 mol NaCl  $\approx$  2 mol particles

$CaCl_2(aq)$



1 mol  $CaCl_2 \approx$   
3 mol particles

### Van't Hoff factor, $i$

$i = 1$  for non-electrolyte

$i = 2$  for 1:1 electrolytes ex: NaCl, KBr,  $NH_4NO_3$

$i = 3$  for 1:2 or 2:1 electrolytes ex:  $CaCl_2$ ,  $Na_2SO_4$



$i = 1$

$i = 2$

$i = 1.05$  ( $i$  does not have to be a whole number)

For very concentrated solutions  $i$  can be less than 2 or 3 (tight ion pairs)

## Colligative properties

1. Vapor pressure lowering
2. Freezing point lowering
3. Boiling point raising
4. Osmotic pressure

### Vapor pressure lowering (Raoult's law)

$$P_{\text{sol'n}} = P_{\text{solvent}} * X_{\text{solvent}}$$

Given the vapor pressure of water is 23.76 mmHg at 25°C. If 17.0g  $C_6H_{12}O_6$  (glucose),  $MM = 180g/mol$  is dissolved in 80.0g  $H_2O$ , what is  $P_{\text{sol'n}}$ ?  
Glucose is a non-volatile, non-electrolyte.

$$\begin{aligned} P_{\text{sol'n}} &= P_{H_2O} * X_{H_2O} \\ &= 23.76 \text{ mmHg} * 0.979 \\ &= \boxed{23.27 \text{ mmHg}} \end{aligned}$$

$$\begin{aligned} X_{H_2O} &= \frac{n_{H_2O}}{n_{H_2O} + n_{C_6H_{12}O_6}} \\ n_{H_2O} &= 4.44 \text{ mol} \\ n_{glc} &= 0.0944 \text{ mol} \\ X_{H_2O} &= \frac{4.44 \text{ mol}}{4.44 \text{ mol} + 0.0944 \text{ mol}} = 0.979 \end{aligned}$$

The more solute that is added the more the vapor pressure decreases

• Suppose 35.0g  $NaCl$  were dissolved in  $H_2O$  at 25°C. What is the  $P_{\text{sol'n}}$ ?  $i=2$

$$\begin{aligned} P_{\text{sol'n}} &= P_{H_2O} * X_{H_2O} \\ P_{\text{sol'n}} &= 23.76 \text{ mmHg} * 0.823 \end{aligned}$$

$$P_{\text{sol'n}} = 19.55 \text{ mmHg}$$

$$\begin{aligned} X_{H_2O} &= \frac{n_{H_2O}}{n_{H_2O} + n_{NaCl} * i} \\ X_{H_2O} &= \frac{5.56}{5.56 + (0.698 * 2)} \end{aligned}$$

$$X_{H_2O} = 0.823$$

- Vapor pressure involving a volatile solute (and volatile solvent)
  - cyclohexane,  $C_6H_{12}$   $MM = 84 \text{ g/mol}$  higher BP  $P_{\text{vap}} = 122 \text{ mmHg}$
  - cyclopentane,  $C_5H_{10}$   $MM = 70 \text{ g/mol}$  higher vapor pressure  $P_{\text{vap}} = 385 \text{ mmHg}$   
at  $30^\circ\text{C}$

$$P_{\text{soln}} = P_A \times X_A + P_B \times X_B$$

$\underbrace{\hspace{100px}}_{\text{cyclopentane}}$ 
 $\underbrace{\hspace{100px}}_{\text{cyclohexane}}$

What is  $P_{\text{soln}}$  made of 4.7 mol cyclohexane and 1.3 mol cyclopentane?

$$X_{\text{cyclopentane}} = \frac{1.3}{1.3 + 4.7} = 0.217$$

$$X_{\text{cyclohexane}} = 1 - 0.217 = 0.783$$

$$P_{\text{soln}} = 0.217 \times 385 \text{ mmHg} + 0.783 \times 122 \text{ mmHg}$$

$$P_{\text{soln}} = 179 \text{ mmHg}$$

- Continuing with the cyclopentane, cyclohexane problem, at  $30^\circ\text{C}$ , what is the composition of a solution that has a vapor pressure of 200 mmHg?

$$P_{\text{soln}} = P_{\text{cyclopentane}} \times X_{\text{cyclopentane}} + P_{\text{cyclohexane}} \times X_{\text{cyclohexane}}$$

$$200 \text{ mmHg} = 385 \text{ mmHg} \times X_{\text{cyclopentane}} + 122 \text{ mmHg} \times (1 - X_{\text{cyclopentane}})$$

$$X_{\text{cyclopentane}} = 0.297$$

### Freezing point lowering

$$\Delta T_f = \text{how much the freezing point is lowered} = K \times m \times i$$

(deg)  $\leftarrow$  either  $^\circ\text{C}$  or  $\text{K}$

constant  
for each solvent  
p. 470

$\leftarrow$  Van't Hoff

questions that could be asked:

what is the change in temperature ( $\Delta T$ )

what is the actual temperature ( $T_{\text{freezing}} - \Delta T$ )



What is  $T_{fp}^{sol'n}$  if 22.4g urea,  $\overbrace{CO(NH_2)_2}^{\text{non-electrolyte}}$   $MM = 60g/mol$  are dissolved in 50g  $H_2O$ ? Given  $K_f(H_2O) = 1.86 \text{ deg/molal}$

$$\Delta T_f = K_f \times m \times i$$

$$m_{urea} = \frac{22.4 \text{ g urea}}{0.050 \text{ kg } H_2O} = 7.47 \text{ molal}$$

$$\Delta T_f = 1.86 \frac{\text{deg}}{\text{molal}} \times 7.47 \text{ molal} \times 1 = 13.9 \text{ deg}$$

$$T_{fp}^{H_2O} = 0^\circ C$$

$$T_{fp}^{sol'n} = 0^\circ C - 13.9^\circ C = \boxed{-13.9^\circ C}$$

• Suppose 4.845g of an unknown  $\overbrace{\text{non-electrolyte}}^{i=1}$  was dissolved in 25.0g  $H_2O$  and the solution froze at  $-4.3^\circ C$ . What is the molar mass of the unknown?

$$MM = \frac{m_{unk}}{n_{unk}} = \frac{4.845 \text{ g}}{0.0578 \text{ mol}} = \boxed{84.3 \text{ g/mol}}$$

$$\Delta T_f = 4.3 \text{ deg} = 1.86 \frac{\text{deg}}{\text{molal}} \times \frac{n_{unk}}{0.025 \text{ kg}} \times 1$$

$$n_{unk} = 0.0578 \text{ mol}$$