

Today, Jan. 24 Section 13.3-13.6

lab tomorrow



expt	time	$[\text{CH}_3\text{CHO}]_0$	initial rate
1	0	1.65M	5.45 mmol/L·s
2	0	4.11M	33.78 mmol/L·s
3	0	6.60M	87.1 mmol/L·s

$$\text{rate} = k [\text{CH}_3\text{CHO}]^{0.1,2}$$

$$5.45 = k [1.65]^{0.1,2}$$

$$33.78 = k [4.11]^{0.1,2}$$

$$\frac{5.45}{33.78} = \frac{1.65^{0.1,2}}{4.11^{0.1,2}}$$

$$0.161 = (0.401)^{0.1,2}$$

$$0.161 = (0.401)^2$$

$$\text{rate} = k [\text{CH}_3\text{CHO}]^2$$

$$33.78 \text{ mmol/L}\cdot\text{s} = k \left(4.11 \frac{\text{mol}}{\text{L}}\right)^2$$

$$33.78 \times 10^{-3} \frac{\text{mol}}{\text{L}\cdot\text{s}} = k \left(4.11 \frac{\text{mol}}{\text{L}}\right)^2$$

$$k = \frac{3.378 \times 10^{-2} \text{ mol} \cdot \text{L}^2}{\text{L}\cdot\text{s} \cdot 4.11^2 \text{ mol}^2} = 0.00200 \frac{\text{L}}{\text{mol}\cdot\text{s}}$$

2nd order

$$\text{rate} = k [A]^2$$

$$\frac{\text{mol}}{\text{L}\cdot\text{time}} = \left(\frac{\text{L}}{\text{mol}\cdot\text{time}}\right) \frac{\text{mol}^2}{\text{L}^2}$$

1st order

$$\text{rate} = k [A]^1$$

$$\frac{\text{mol}}{\text{L}\cdot\text{time}} = \left(\frac{1}{\text{time}}\right) \frac{\text{mol}}{\text{L}}$$

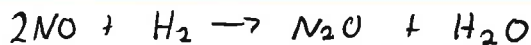
0 order

$$\text{rate} = k [A]^0$$

$$\frac{\text{mol}}{\text{L}\cdot\text{time}} = \left(\frac{\text{mol}}{\text{L}\cdot\text{time}}\right)$$

the units for k can change

$$\text{rate} = k [A]^{0,1, \text{ or } 2} \times [B]^{0,1, \text{ or } 2}$$



expt	[NO] ₀	[H ₂] ₀	initial rate
1	0.60	0.37	0.181
2	1.00	0.37	0.503
3	0.60	0.94	0.181

$$\text{rate} = k (\text{NO})^{0,1,2} (\text{H}_2)^{0,1,2}$$

$$\frac{0.181}{0.503} = k \left(\frac{0.60}{1.00}\right)^{0,1,2} \times \left(\frac{0.37}{0.37}\right)^{0,1,2}$$

$$0.358 = (0.6)^{0,1,2}$$

$$0.36 = (0.6)^2$$

2nd order

Rate law: $\text{rate} = k [\text{NO}]^2$

$$\text{rate} = k (\text{NO})^{0,1,2} (\text{H}_2)^{0,1,2}$$

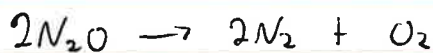
$$\frac{0.181}{0.181} = k \left(\frac{0.60}{0.60}\right)^{0,1,2} \times \left(\frac{0.37}{0.94}\right)^{0,1,2}$$

$$1 = (0.39)^{0,1,2}$$

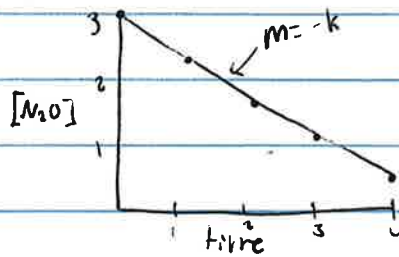
$$1 = (0.39)^0$$

zero order

(since H₂ is to zero order you don't have to write it)



time	[N ₂ O]
→ 0 hrs	3.00 mol/L
1 hr	2.37
→ 2 hrs	1.74
3 hrs	1.11
4 hrs	0.48



$$y = mx + b$$

$$[\text{N}_2\text{O}]_t = m(t) + [\text{N}_2\text{O}]_0$$

negative

k = always positive

$$k = -m$$

time concentration expression

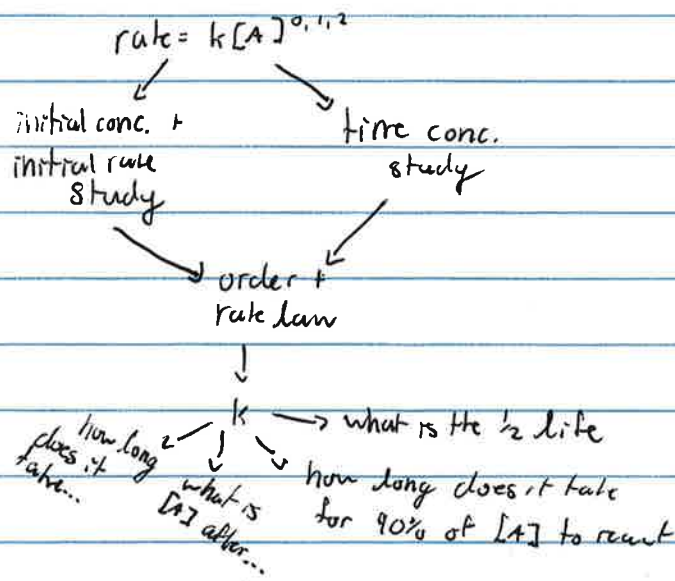
for zero order:

$$[A]_t = -k(t) + [A]_0$$

to find slope pick 2 times (usually $t=0$ and then pick another where the concentration is about half the initial concentration)

$$1.74 \text{ mol/L} = -k(2\text{hr}) + 3.00 \frac{\text{mol}}{\text{L}}$$

$$k = 0.63 \frac{\text{mol}}{\text{L}\cdot\text{hr}}$$



How long does it take until $[N_2O] = 1.50 \text{ mol/L}$

$$1.50 \frac{\text{mol}}{\text{L}} = -0.63 \frac{\text{mol}}{\text{L}\cdot\text{hr}} (t) + 3.00 \frac{\text{mol}}{\text{L}}$$

$$t = 2.38 \text{ hrs.}$$

What is $[N_2O]$ after 45 min?

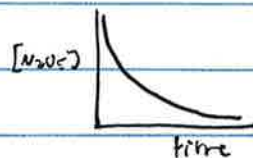
$$\frac{45 \text{ min}}{60 \text{ min}} = 0.75 \text{ hr}$$

$$[N_2O]_{0.75 \text{ hr}} = -0.63 \frac{\text{mol}}{\text{L}\cdot\text{hr}} (0.75 \text{ hr}) + 3.00 \frac{\text{mol}}{\text{L}}$$

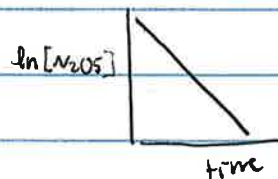
$$[N_2O]_{0.75 \text{ hr}} = 2.53 \frac{\text{mol}}{\text{L}}$$



time	$[N_2O_5]$	$\ln [N_2O_5]$
0s	2.330 mol/L	0.846
1000s	1.260 mol/L	0.231
2000s	0.681 mol/L	-0.384
3000s	0.369 mol/L	-0.997



zero order ✗



first order ✓

$$y = mx + b$$

$$\ln [N_2O_5]_t = m(t) + \ln [N_2O_5]_0$$

$$y = mx + b$$

$$\ln [N_2O_5]_t = -kt + \ln [N_2O_5]_0$$

$$-kt = \ln [N_2O_5]_t - \ln [N_2O_5]_0$$

$$kt = \ln \left(\frac{[N_2O_5]_0}{[N_2O_5]_t} \right)$$

$$\ln \left(\frac{[A]_0}{[A]_t} \right) = kt = \ln \left(\frac{[A]_0}{[A]_t} \right) = -kt \quad \left. \vphantom{\ln \left(\frac{[A]_0}{[A]_t} \right)} \right\} \begin{array}{l} \text{time-conc} \\ \text{expression for} \\ \text{1st order} \end{array}$$

how long does it take for $[N_2O_5]$ to decrease to 1.50 mol/L?

$$\ln \left(\frac{[A]_0}{[A]_t} \right) = kt$$

$$\ln \left(\frac{2.330 \text{ mol/L}}{0.681 \text{ mol/L}} \right) = k(2000 \text{ s})$$

$$k = 0.00062 = 6.15 \times 10^{-4} \text{ s}^{-1}$$

$$\ln \left(\frac{2.330 \text{ mol/L}}{1.50 \text{ mol/L}} \right) = (6.15 \times 10^{-4} \text{ s}^{-1})t$$

$$t = 716 \text{ s}$$

what is $[N_2O_5]$ after 2500s?

$$\ln \left(\frac{2.330 \text{ mol/L}}{[N_2O_5]_{2500 \text{ s}}} \right) = (6.15 \times 10^{-4} \text{ s}^{-1})(2500 \text{ s})$$

$$[N_2O_5]_{2500 \text{ s}} = 0.501 \text{ mol/L}$$

How long does it take for 32% of the $[N_2O_5]$ to react?

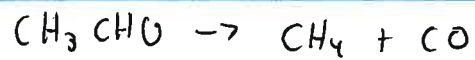
$$\ln \left(\frac{100\%}{68\%} \right) = kt$$

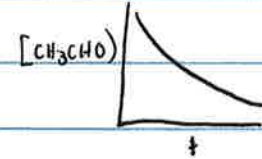
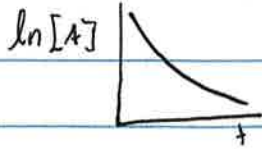
$$t = 627 \text{ s}$$

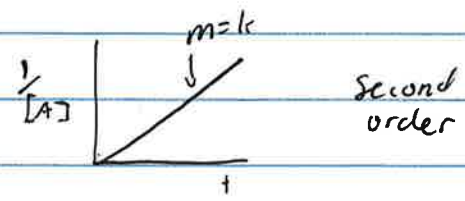
How long does it take until $[N_2O_5]$ falls to 75% of its original value?

$$\ln \left(\frac{100\%}{75\%} \right) = kt$$

$$t = 490 \text{ s}$$



time	$[\text{CH}_3\text{CHO}]$	$[\text{CH}_3\text{CHO}]$	
0 hr	0.400 mol/L		not zero order
3 hr	0.118		
6 hr	0.069		not first order
9 hr	0.049		
12 hr	0.038		



time conc expression
for second order:

$$\frac{1}{[A]_t} = \frac{k}{[A]_0} t + \frac{1}{[A]_0}$$